

# Mark Scheme (Results)

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Pearson Edexcel International GCSE Mathematics B (4MB0)
Paper 02



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# **General Marking Guidance**

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme.
  - Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

# Types of mark

- o M marks: method marks
- o A marks: accuracy marks
- o B marks: unconditional accuracy marks (independent of M marks)

#### **Abbreviations**

- o cao correct answer only
- $\circ$  ft follow through
- o isw ignore subsequent working
- o SC special case
- o oe or equivalent (and appropriate)
- o dep dependent
- o indep independent
- o eeoo each error or omission

### No working

- If no working is shown then correct answers normally score full marks
- If no working is shown then incorrect (even though nearly correct) answers score no marks.

## With working

- If there is a wrong answer indicated on the answer line always check the working in the body of the script (and on any diagrams), and award any marks appropriate from the mark scheme.
- If it is clear from the working that the "correct" answer has been obtained from incorrect working, award 0 marks.
- Any case of suspected misread loses A (and B) marks on that part, but can gain the M marks.
- If working is crossed out and still legible, then it should be given any appropriate marks, as long as it has not been replaced by alternative work.
- If there is a choice of methods shown, then no marks should be awarded, unless the answer on the answer line makes clear the method that has been used.
- If there is no answer on the answer line then check the working for an obvious answer.

# **Ignoring subsequent work**

- It is appropriate to ignore subsequent work when the additional work does not change the answer in a way that is inappropriate for the question: eg. Incorrect cancelling of a fraction that would otherwise be correct.
- It is not appropriate to ignore subsequent work when the additional work essentially makes the answer incorrect eg algebra.
- Transcription errors occur when candidates present a correct answer in working, and write it incorrectly on the answer line; mark the correct answer.

## Parts of questions

• Unless allowed by the mark scheme, the marks allocated to one part of the question CANNOT be awarded in another.

Question	Working	Answer	Mark	Notes
1(a) (i)	6.3×50	310 - 320	2	B1
(ii)		302° ± 2°		B1
(b)	Constructs perpendicular bisector of line AC		2	B1
	Draws circle (or two arcs crossing their perpendicular bisector) with radius 4.5 cm from centre <i>B</i>			B1
(c)		016° - 018°	1	B1
2 (a)	$f(-1) = (-1)^3 - (-1)^2 + k(-1) - 24 = 0 \Rightarrow k = -26$	k = -26	2	M1A1
(b)	$(x^{3}-x^{2}-26x-24) \div (x+1) = (x^{2}-2x-24)$ $(x^{2}-2x-24) = (x+4)(x-6)$ $(x^{3}-x^{2}-26x-24)$	(x+1)(x+4)(x-6)	4	M1A1 $(x^2 - 2x \pm k)$ [Compare coefficients $A = 1, B = -2$ ]
	$(x^2-2x-24)=(x+4)(x-6)$			M1
	$(x^3-x^2-26x-24)$			A1
	,			

Question	Working	Answer	Mark	Notes
3 (a)	$\left[S.A. = 2\pi rh + 2\pi r^2\right]$	15	3	M1
	$252\pi = 2 \times 6 \times \pi \times h + 2 \times 6^2 \times \pi$			M1A1
	$\Rightarrow 252 = 12h + 72 \Rightarrow 180 = 12h \Rightarrow h = 15$			
(b)	$V = \pi \times 6^2 \times 15 = 540\pi$	7.4 [cm]	4	M1A1
	$540\pi = \frac{4}{3} \times \pi \times r^3 \Rightarrow r^3 = 405 \Rightarrow 7.3986 \approx 7.4 \text{ [cm]}$			M1A1
4 (a)	$36 \times 7.60 + \frac{4}{100} \times 4250$	\$443.60	2	M1A1
(b)	$430.8 = 41 \times 7.6 + \frac{4}{100} \times N$	\$2980	2	M1A1
	$\Rightarrow N = 119.2 \times 100 \div 4$			
(c)	$1.051 \times 1.045^2 = 1.147718$	\$1850	3	M1
	2123.28÷'1.147718'=1850			M1
				A1

Question	Working	Answer	Mark	Notes
5 (a)	$t = 3 \Rightarrow s = (3)^3 - 9(3)^2 + 15 \times 3 + 6 = -3$	-3 m	2	M1A1 (Allow 3 m)
(b) (i)	$v = \left(\frac{\mathrm{d}s}{\mathrm{d}t}\right) = 3t^2 - 18t + 15$	<i>t</i> = 1, 5	4	M1A1 M1
	$v = 0$ $3t^{2} - 18t + 15 = 0 \Rightarrow \left[t^{2} - 6t + 5\right] = (t - 1)(t - 5) = 0$ $\Rightarrow t = \dots, \dots$			A1
(c)	$a = \left(\frac{dv}{dt}\right) = 6t - 18$ $t = 4 \Rightarrow a = 24 - 18$	$a = 6 \ (m/s^2)$	3	M1 M1 A1

Question		Working			Answer	Mark	Notes
6 (a)	Table				(i) 10	1	B1
	Weight (x g)	Frequency	Class width	FD			
	$20 < x \le 30$	16	10	1.6			
	$30 < x \le 35$	28	5	5.6			
	$35 < x \le 40$	32	5	6.4			
	$40 < x \le 50$	14	10	1.4			
	$50 < x \le 70$	10	20	0.5			
	(50, 0.5) (70, 0.3)	5)			(ii)	3	B1 for calculating scale . FD of 1 = 5 small squares.  B1 one bar correct B1 for all three correct

Question	V	Vorking		_	Answer	Mark	Notes
(b)					37.4	M1	Uses correct midpoints
(0)	Weight (x g)	Frequency	Mid Points	Total		M1	For attempting to use
	$20 < x \le 30   16   25   400$	M1	$\sum \frac{\text{frequency} \times \text{'their' midpoint}}{100}$				
	$30 < x \le 35$	28	32.5	910		A1	
	$35 < x \le 40$	32	37.5	1200			For fully correct $\sum \frac{\text{frequency} \times \text{midpoints}}{100}$
	$40 < x \le 50$	14	45	630			
	$50 < x \le 70$	10	60	600			100
			Total	3740			
	Estimate of Mean = $\frac{3740}{100}$ = 37.4					A1 (4)	For 37.4

Question	Working	Answer	Mark	Notes
7(a)	$0.4 \times P$ (he is late when he catches the bus) = 0.1	0.25	2	M1A1
	$\Rightarrow$ P(he is late when he catches the bus) = $\frac{0.1}{0.4}$ = 0.25			
(1-)			3	B1 – any 2 values correct
(b)				B1 – any 3 values correct
	'0.25'			B1 – all 5 values correct ft their 0.25
	0.4 1 - '0.25' l'			
	0.6			
	0.05 1 w			
	0.95			
(c)	$0.6 \times 0.95 + 0.4 \times '0.75' = 0.87$	0.87	2	M1A1ft

Question	Working	Answer	Mark	Notes
8(a)		Rotation 90° clockwise	3	B1 (More than one transformation Scores 0/3 marks) B1
(b)	Vertices at $(4, -3), (4.5, -5) (2.5, -4)$	Centre (1,1)  Correct diagram	3	M1 – for a similar shape in the second quadrant in the correct orientation M1 – for an image in the correct orientation of the correct size A1 cao
(c)	METHOD 1 $\begin{pmatrix} 0 & -2 \\ -2 & 1 \end{pmatrix} \begin{pmatrix} a & b & c \\ d & e & f \end{pmatrix} = \begin{pmatrix} -2 & 0 & 2 \\ 3 & 7 & 4 \end{pmatrix}$	$(-1, 1), \left(-\frac{7}{2}, 0\right), \left(-\frac{5}{2}, -1\right)$	4	M1 - for attempting to premultiply the matrix for triangle $D$ by $T$
	$0 \times a - 2 \times d = -2 \Rightarrow d = 1$ $0 \times b - 2 \times e = 0 \Rightarrow e = 0$ $0 \times c - 2 \times f = 2 \Rightarrow f = -1$			A1 – for correct multiplication of matrix (Co-ords in any order- but must be consistent)
	$-2a+d=3 \Rightarrow a=-1$ $-2b+e=7 \Rightarrow b=-\frac{7}{2}$ $-2c+f=4 \Rightarrow c=-\frac{5}{2}$			M1 – solves the equations to find values for <i>a</i> , <i>b</i> , <i>c</i> , <i>d</i> , <i>e</i> and <i>f</i> .  A1 – for correct coordinates of triangle <i>D</i>

METHOD 2	$(-1, 1), \left(-\frac{7}{2}, 0\right), \left(-\frac{5}{2}, -1\right)$	M1 – for finding the correct determinant (–4)
Finds the inverse of <b>T</b>		A1 – for finding $\mathbf{T}^{-1}$
$\begin{pmatrix} 0 & -2 \\ -2 & 1 \end{pmatrix}^{-1} = -\frac{1}{4} \begin{pmatrix} 1 & 2 \\ 2 & 0 \end{pmatrix}$ $-\frac{1}{4} \begin{pmatrix} 1 & 2 \\ 2 & 0 \end{pmatrix} \begin{pmatrix} -2 & 0 & 2 \\ 3 & 7 & 4 \end{pmatrix} = \begin{pmatrix} -1 & -\frac{7}{2} & \frac{-5}{2} \\ 1 & 0 & -1 \end{pmatrix}$		M1 – for multiplying $\mathbf{T}^{-1} \times \text{coords of triangle } A$ A1 – for correct coordinates of triangle $D$ $\text{Accept} \begin{pmatrix} -1 & -3.5 & -2.5 \\ 1 & 0 & -1 \end{pmatrix} \text{ for A1}$

Question	Working	Answer	Mark	Notes
9(a)	$AC = \sqrt{10^2 + 10^2} = 10\sqrt{2} \Rightarrow EO = 5\sqrt{2}$ $EO = \sqrt{15^2 - (5\sqrt{2})^2} = \sqrt{175} = 5\sqrt{7}$	*	3	M1 M1A1 Penalise incorrect rounding once only in this question
(b)	$\angle EMO = \tan^{-1} \left( \frac{5\sqrt{7}}{5} \right) = 69.2951 \approx 69.3^{\circ}$	69.3°	2	M1A1
(c)	$a^{2} = b^{2} + c^{2} - 2bc \cos A \Rightarrow \cos A = \frac{b^{2} + c^{2} - a^{2}}{2bc}$ $\angle AEB = \cos^{-1}\left(\frac{15^{2} + 15^{2} - 10^{2}}{2 \times 15 \times 15}\right) = 38.942 \approx 38.9^{\circ}$	38.9°	3	M1 M1A1
(d)	Area of $\angle AEB = \frac{1}{2} \times 15 \times 15 \times \sin 38.942 = 70.710$ Area of base = $10 \times 10 = 100$ Total surface area = $4 \times 70.710 + 10 \times 10 = 382.8$ [cm <sup>2</sup> ]	383 [cm <sup>2</sup> ]	4	M1 B1 M1A1

Question	Working	Answer	Mark	Notes
10 (a)(i) (ii)	$\overrightarrow{OQ} = \overrightarrow{OA} + \frac{2}{5}\overrightarrow{AB} \Rightarrow \overrightarrow{OQ} = \frac{12}{5}\mathbf{a} + \frac{6}{5}\mathbf{b}$	$\overrightarrow{PB} = 3\mathbf{b} - 2\mathbf{a}$ $\overrightarrow{OQ} = \frac{12}{5}\mathbf{a} + \frac{6}{5}\mathbf{b}$	3	B1 M1A1
(b) (i) (ii)	$\overrightarrow{OX} = \lambda \left( \frac{12}{5} \mathbf{a} + \frac{6}{5} \mathbf{b} \right) \text{ and } \overrightarrow{PX} = \mu \left( -2\mathbf{a} + 3\mathbf{b} \right)$ $\overrightarrow{AX} = -4\mathbf{a} + \lambda \left( \frac{12}{5} \mathbf{a} + \frac{6}{5} \mathbf{b} \right)$ $\overrightarrow{AX} = -2\mathbf{a} + \mu \left( -2\mathbf{a} + 3\mathbf{b} \right)$	$\overrightarrow{AX} = -4\mathbf{a} + \lambda \left(\frac{12}{5}\mathbf{a} + \frac{6}{5}\mathbf{b}\right)$ $\overrightarrow{AX} = -2\mathbf{a} + \mu(-2\mathbf{a} + 3\mathbf{b})$	4	M1A1 M1A1
(c)	Equates components $-4\mathbf{a} + \lambda \left(\frac{12}{5}\mathbf{a} + \frac{6}{5}\mathbf{b}\right) = -2\mathbf{a} + \mu(-2\mathbf{a} + 3\mathbf{b})$		3	M1 M1A1
	$\Rightarrow \frac{6}{5}\lambda = 3\mu \text{ and } \frac{12}{5}\lambda = 2 - 2\mu$ Solves simultaneous equations $\lambda = \frac{5}{8} \qquad \mu = \frac{1}{4}$	$\lambda = \frac{5}{8} \qquad \mu = \frac{1}{4}$		

(d)	$\frac{\Delta AOX}{\Delta AXQ} = \frac{5}{3}$	$\frac{25}{3}$ (units <sup>2</sup> )	3	M1 M1A1
	Area $\triangle AOX = \frac{5}{3} \times 10 = \frac{50}{3}$			
	Area $\triangle OPX = \frac{1}{2} \times \triangle AOX = \frac{1}{2} \times \frac{50}{3} = \frac{25}{3}$ (units <sup>2</sup> )  ALT  Area of $\triangle OPX$ Area of $\triangle OAQ$ Area of $\triangle AXQ$ Area of $\triangle AXQ$ Area of $\triangle AOQ$ $= \frac{2 \times 3}{2 \times 8} = \frac{3}{8}$	$\frac{25}{3}$ (units <sup>2</sup> )	{3}	{M1 M1 A1}
	As $\triangle AXQ = 10$ it follows that $Area \text{ of } \triangle AOQ = \frac{80}{3}$ And Area of $\triangle OPX = \frac{5}{16} \times \frac{80}{3} = \frac{25}{3}$			

Question	Working	Answer	Mark	Notes
11 (a)	$24 = 2x^2y \Rightarrow y = \frac{24}{2x^2} = \left(\frac{12}{x^2}\right)$	$y = \frac{24}{2x^2} = \left(\frac{12}{x^2}\right)$	2	M1A1
(b)	$S = 4x^{2} + 6xy$ $S = 4x^{2} + 6x \times \frac{12}{x^{2}} \Rightarrow S = 4x^{2} + \frac{72}{x}$	$S = 4x^2 + \frac{72}{x}$	2	M1A1
(c)	$\left(S = 4x^{2} + 72x^{-1}\right)$ $\frac{dS}{dx} = 8x - 72x^{-2}$	x = 2.08 (cm)	4	M1A1
	$\frac{dx}{dx} = 6x - 72x$ $8x - 72x^{-2} = 0 \Rightarrow 8x = \frac{72}{x^2}$ $x^3 = 9 \Rightarrow x = 2.08 \text{ (cm)} \qquad *$			M1A1
(d)	$S = 4 \times 2.08^2 + \frac{72}{2.08} = 51.9209 = 51.9 \text{ (3sf)}$	$S = 51.9 \text{ (cm}^2\text{)}$	1	B1

(e)				60, 70	2	B1B1
	x	3	3.5			
	$4x^2$	36	49			
	72	24	20.6			
	x S	60	70			
<b>(f)</b>	Graph penalties (-1) Straight line segments Each point missed $(\pm \frac{1}{2} \text{ small square})$ Each point not plotted Tramlines Very poor curve ie., line too thick				3	B3 (Graph penalties)
(g)	Line drawn or two points marked consistent with line		1.2±0.2 3.3±0.2	2	B1ft $1.2 < x$ B1ft $x < 3.3$	
	Correct region values from the		$\langle x \langle 3.3  $ ft their			